Excitonic Lasers in Atomically Thin 2D Semiconductors

Wen Wen, Lishu Wu, and Ting Yu*

ABSTRACT: Two-dimensional (2D) atomically thin transition-metal dichalcogenides (TMD) and their van der Waals (vdW) heterostructures offer a platform with tightly bound intralayer/interlayer excitons for the on-chip fabrication of ultracompact nanolasers. Excitons in 2D TMD materials present a considerable binding energy of up to hundreds of meV, which permits a high Mott transition density of $10^{14}$ cm$^{-2}$ and stable excitonic lasing under room-temperature operation and high pump fluences. Here, we review the recent progress on the lasing emission from intralayer excitons in TMD monolayers and interlayer excitons in vdW heterostructures incorporated with various high-quality optical cavities, including photonic-crystal, whispering-gallery-mode, distributed-feedback, distributed-Bragg-reflector cavities. Lasing emissions in TMD monolayers and heterostructures have been demonstrated by narrow emission peaks, a clear threshold for nonlinear amplification, time- and spatial coherence under either continuous-wave or pulsed light pumping. Finally, prospective and frontier research topics, including large-scale on-chip integration of TMD nanolasers, electrically pumped lasers, spin-polarized nanolasers, and exciton–polariton Bose–Einstein condensation (BEC) are highlighted.

The considerably high exciton binding energy in TMD monolayers permits stable excitons under relatively high population and sustains excitonic lasing emissions.

Provided a novel platform to investigate the exciton excited states, carrier dynamics, spin–valley coupling and moiré potentials. Meanwhile, vdW heterostructures also offer a new paradigm to design the superior properties of materials and functionalities of devices because the material properties can be tuned by constituent layers, stacking sequence, crystallographic orientation, and external fields. In the vdW heterostructures composed of TMDs, interlayer excitons can be created through either ultrafast charge transfer in optical...
EXCITONS IN TMD MONOLAYERS AND HETEROSTRUCTURES

The excitons in TMD monolayers and heterostructures have attracted intense attention owing to the following features. First, TMDs undergo a transition from an indirect to a direct bandgap, when the thickness of TMDs is thinned down to monolayers (Figure 1a), which is reflected by a great enhancement of PL quantum efficiency with a factor of exceeding 104 in monolayers.

Second, the stable excitons with a large binding energy of hundreds of meV have been demonstrated, which is attributed to the quantum confinement effect and significantly reduced dielectric screening in TMD monolayers (Figure 1b–d). The n = 3−5 peaks can be fitted by a 2D hydrogen model. Exciton transition energies can be calculated by bandgap ($E_b$) and exciton binding energy of nth excitonic state ($E_b^{(n)}$) as $E_b^{(n)} = E_b - E_b^{(n-1)}$ (1).

excitation process or direct electrical injection of electrons/holes into two separated layers.57,59−61 Compared to their intralayer counterparts, interlayer excitons feature longer lifetime,57 directional dipole,52 and longer valley polarization lifetime,60 which allow for the long-range exciton diffusion, tunable carrier dynamics by electrostatic gating and manipulation of spin-polarized carriers at different valleys.52,58,61,62

In addition, on the basis of these atomically thin materials with tightly bound excitons, ultracompact on-chip lasers have been developed. In 2015, the first demonstration of lasing emissions was reported in WSe2 incorporated with a photonic crystal cavity.18 After then, the lasing emissions of TMD monolayers and heterostructures have been also implemented by using photonic-crystal33,63,64 distributed-feedback53 distributed-Bragg-reflector,65 and whispering-gallery-mode cavities.54,67 By the material engineering and optical cavity optimization, continuous-wave lasing emissions with a relatively low threshold at room temperature have been realized on both monolayers and vdW heterostructures. In this Review, we summarize recent progress in atomically thin 2D nanolasers based on TMD monolayers and heterostructures. Firstly, we briefly introduce the properties of intralayer excitons in TMD monolayers and interlayer excitons in vdW heterostructures. Secondly, the atomically thin lasers based on intralayer excitons and various optical cavities are discussed. Thirdly, lasing emission and Bose–Einstein condensation (BEC) from interlayer excitons in vdW heterostructures are discussed. We describe the material fabrication, optical cavity design, and lasing performance of lasers based on TMD monolayers and heterostructures. The lasing emissions in TMD materials have been characterized by a narrowed peak, a threshold in the output intensity, and emergent spatial coherence. We conclude the Review by highlighting the future research directions, including exciton–polariton lasers, spin lasers, electrically pumped lasers and scalable fabrication of lasers based on TMD materials.
where $\mu$ is the reduced mass of exciton and $\varepsilon$ is the permittivity. The model is well fitted with $n = 3$–5 excitons and indicates a bandgap of $E_g = 2.41 \pm 0.04$ eV, and the exciton binding energy of the 1s exciton state is $0.32 \pm 0.04$ eV by considering its exciton transition energy of $2.09$ eV (Figure 1c). The non-hydrogenic physics of $n = 1$, 2 excitons are caused by the higher effective dielectric constants of excitons with low quantum numbers (Figure 1c inset). Shan and her colleagues demonstrated the measurement of band-to-band transition in WSe$_2$ monolayers by combining linear absorption and two-photon PL (2PPL) excitation spectra (Figure 1d). While linear absorption could not identify a clear band-to-band transition, the 2PPL excitation spectrum can be well fitted by an exciton peak related to the superposition of 3 states and a band-to-band transition with $E_g = 2.02$ eV. The binding energy of 1s excitons was calculated as 0.37 eV based on the 1s exciton transition energy and band-to-band transition energy. The considerable high exciton binding energy in TMD monolayers permits stable excitons under relatively high population and sustains excitonic lasing emissions.

Third, broken inversion symmetry and strong spin–orbit coupling cause spin–valley locking, which gives rise to intriguing properties, such as valley Hall effect, valley polarized excitons, valley Zeeman, and AC stark effects. Valley polarized lasing emission has yet been realized in TMDs possibly because of the depolarization caused by the electron–hole exchange interaction, which is enhanced under high exciton population. Therefore, in this Review, we will not further discuss the spin–valley polarization and some comprehensive reviews on this topic are recommended.

Fourth, atomically sharp heterostructures can be constructed by stacking different kinds of TMD layers. The library of 2D TMDs allows for constructing type-II heterostructures, which support ultrafast charge transfer and formation of interlayer excitons. Density functional theory (DFT) calculations have been performed to predict the band edges of TMD monolayers, which has provided guidelines for the construction of type-II heterostructures (Figure 1e). Before the discovery of interlayer excitons, the ultrafast charge transfer has been demonstrated by Wang and his colleagues in type-II MoS$_2$/WS$_2$ heterolayers. PL mapping demonstrated a strongly quenched PL in the heterostructure region, indicating the efficient charge transfer. By using femtosecond pump-probe spectroscopy, ultrafast hole transfer from MoS$_2$ to WS$_2$ at a time scale of within 50 fs has been revealed. The ultrafast charge transfer in heterostructures enables the buildup of a high population of interlayer excitons before the recombination of intralayer excitons.

The ultrafast charge transfer in heterostructures enables the buildup of a high population of interlayer excitons before the recombination of intralayer excitons. Xu and his colleagues firstly reported the formation of interlayer excitons between WSe$_2$–MoSe$_2$ heterolayers (Figure 1f). PL spectrum of WSe$_2$–MoSe$_2$ shows an interlayer exciton peak at lower energy of 1.4 eV, while the emissions of neutral (X') and charged (X'') excitons range from 1.55 to 1.75 eV. Interlayer excitons with electrons in MoSe$_2$ and holes in WSe$_2$ exhibit directional dipoles from MoSe$_2$ to WSe$_2$, which supports tuning of excitonic emission by electric field (Figure 1g). Compared to the rapid exciton recombination with the lifetime of 3–100 ps, the interlayer excitons present a much longer lifetime of over 1 $\mu$s (Figure 1h). More importantly, exciton–hole exchange interaction for the depolarization process is suppressed owing to the spatial separation of electrons and holes, yielding an ultralong valley polarization lifetime of 40 $\mu$s. Interlayer excitons with electrons and holes in two separated layers have been demonstrated with longer carrier lifetime, valley polarization lifetime, tunable polarization by electric field and controllable carrier species and dynamics through electrical injection. Therefore, interlayer excitons are promising candidates to be used in spin lasers and electrically pumped lasers based on TMD heterostructures.

### Lasing Emission in TMD Monolayers

Lasers comprise gain media for stimulated photon emission and optical cavities for confinement and resonant recirculation of light. As an ultrathin quantum emitter, monolayer TMD is a category of high-performance gain media with unique advantages of small footprints, low power consumption, efficient coupling with microcavities, and feasible on-chip integration. TMD monolayers possess tightly-bound excitons with binding energy of exceeding 0.3 eV. Such a large binding energy sustain stable excitons at the room temperature and high Mott transition density of $\sim 10^{14}$ cm$^{-2}$. Therefore, stable excitons can be preserved even at the pump fluence level for achieving population inversion. These excitons also possess high radiative recombination quantum efficiency owing to the intrinsic direct bandgap in TMD monolayers. Strong excitonic resonance and small Bohr radius also benefit efficient and fast radiative recombination, which is important for the buildup of population inversion. For TMD monolayer lasers, the design and optimization of optical cavities are crucial for realizing low-threshold lasing emission. Because of their ultrathin size, TMD monolayers are not capable of confining emitted photons, which requires additional optical cavities to sustain high optical gain.

Because of their ultrathin size, TMD monolayers are not capable of confining emitted photons, which requires additional optical cavities to sustain high optical gain. In this section, we will review lasers constructed by TMD monolayers as gain media and different optical cavities. Before the discussion of specific reports, we would like to recommend the Commentary Article on the criteria of lasing emission, which include narrow line width, clear threshold, small beam divergence, polarization, and spatial and temporal coherence.

### Photonic Crystal Lasers

Photonic crystal cavities are usually fabricated by etching periodic structures on membranes with high refractive indexes. These periodic structures show tunable photonic bandgaps, which prevent light propagation at corresponding frequencies. By introducing defects in periodic structures, strong confinement of electromagnetic field can be realized, yielding microcavities with small volumes and large quality factors exceeding $10^4$. Therefore, photonic-crystal cavities have shown broad applications in optically/electrically pumped...
nanolasers, cavity quantum electrodynamics and single-photon sources. The photonic crystal cavities have enabled the fabrication of high-performance nanolasers with low thresholds, high quality factors and ultrafast modulation.80−83 For instance, quantum dots, a kind of quantum emitters with ultrasmall mode volume, have been incorporated into photonic crystal cavities to create nanolasers.84,85 Photonic crystals also provide a platform for the integrated photonics based on 2D materials. Nanolasers, waveguides, interferometers, modulators, and photodetectors can be integrated onto a photonic-crystal chip to build photonic logic devices.32,86,87

The first TMD-monolayer laser was reported by Xu and his colleagues in 2015.33 This nanolaser was constructed by loading a mechanically exfoliated WSe2 monolayer onto a photonic-crystal cavity (Figure 2a, b). To ensure the high gain and low loss, a L3-type photonic crystal cavity was fabricated on a gallium phosphide (GaP) thin membrane, which is transparent to WSe2. This photonic crystal cavity presented a quality factor of about 104, which created strong local optical density of states. Power-dependent PL measurements unambiguously demonstrated lasing emission of this TMD monolayer laser. At 80 and 130 K, a clear "kink" has been observed in the pump-power-dependent output intensity curves (Figure 2c, d). In contrast, the intensities of spontaneous emission presented no obvious "kink" as a function of pump power. The power-dependent intensity can be fitted by the rate equation as follows

\[
\beta = \frac{1}{\Gamma + \Gamma_c + \Gamma_a + \Gamma_{ex}}
\]

where \( \beta \) is the fraction of spontaneous emission into the cavity mode. A \( \beta \) factor of 0.19 is best fitted for the power-dependent output intensity curve. The line width of PL peak is also dependent on the pump power (Figure 2e). With the increase of pump power, line width of PL peak experienced a narrowing from 0.75 to 0.55 nm below the threshold. Across the threshold regime, a slight broadening of line width to 0.65 nm occurred and then the line width continuously decreased to 0.55 nm above the threshold. The broadening of line width in threshold regime can be attributed to the coupling between intensity and phase noise during the transition from spontaneous emission to stimulated emission, which has been observed in other photonic-crystal lasers based on quantum dots and quantum wells. This nanolaser also presented localized lasing emission at the defect sites in the photonic crystal. At the defect site, narrow PL peak related to stimulated emission of WSe2 in cavity can be observed. In contrast, a broad PL peak related to spontaneous emission from WSe2 can be observed in the off-cavity region. This work demonstrated, for the first time, that lasing emission can be realized on an ultrathin quantum emitter with stable excitons.

Silicon photonic crystal cavities are not suitable for the fabrication of nanolasers based on MoS2, WS2, MoSe2, and WSe2 because of the strong absorption of photons with energy higher than 1.1 eV for silicon.

The above reported nanolaser based on WSe2 and GaP photonic crystal cavities can only be operated at cryogenic temperature, as the room-temperature operation of this
nanolaser might be limited by its relatively low quality factor. Silicon exhibits a high refractive index of 3.4 and matured fabrication techniques for the construction of photonic crystal structures. However, silicon photonic cavity is not suitable for the fabrication of nanolasers based on MoS\(_2\), W\(_S\)\(_2\), MoSe\(_2\), and WSe\(_2\), owing to the strong absorption of photons with energy higher than 1.1 eV for silicon. The self-absorption introduces large losses in cavities, which is detrimental to the lasing emission. Ning and his colleagues circumvented this restriction and reported a room-temperature nanolaser based on silicon photonic cavity by employing monolayer MoTe\(_2\) as gain media.\(^6\) Monolayer MoTe\(_2\) exhibits an excitonic emission peak at \(\sim\) 1.1 eV, which is 50 meV below the bandgap of silicon. By covering monolayer MoTe\(_2\) onto silicon photonic crystal (Figure 2f), infrared lasing emissions were realized at room temperature.

The photonic crystal cavity was fabricated by electron-beam lithography and etching on a silicon-on-insulator chip, yielding a suspended nanobeam structure (Figure 2g, inset). This nanobeam cavity contained 10 periods of holes at each side as "mirror" sections, while 8 holes with gradually decreased size served as a cavity. This photonic crystal cavity presents three resonant cavity modes at wavelength of 1054, 1132, and 1167 nm with quality factor of 5.2 \(\times\) 10\(^6\), 6.5 \(\times\) 10\(^5\), and 1.4 \(\times\) 10\(^3\), respectively. An exfoliated MoTe\(_2\) monolayer was directly transferred onto the nanobeam cavity to construct a nanolaser. The nanolaser was pumped by a 633 nm continuous-wave laser at room temperature. With the increase of pumped power, a narrow PL peak at 1132 nm can be observed, indicating the lasing emission (Figure 2g). The full width at half maximum (FWHM) is 0.202 nm, corresponding to a quality factor of 5603. This quality factor is higher than that of 2465 observed in the GaP cavity at cryogenic temperature. The greatly enhanced quality factor enables lasing emission at room temperature. The output intensities present an obvious threshold of 0.097 mW with the increase of pumped power. The output-intensity curve can be fitted by rate equation with a \(\beta\) factor of 0.1. In summary, this work demonstrated a low-threshold infrared laser based on a MoTe\(_2\) monolayer and suspended photonic crystal cavity, which highlights the importance of high-quality factor of cavity to the high-performance nanolasers.

WHISPERING GALLERY MODE LASERS

Whispering gallery mode (WGM) microcavities,\(^7\) such as microdisks, microspheres, and optical fibers, have been demonstrated with ultrahigh quality factor for the application of small lasers,\(^8\) chemical/biological sensors,\(^9\) and frequency combs.\(^10\) Ultrahigh quality factor of exceeding 10\(^8\) have been demonstrated in microdisks and optical fibers,\(^11\) permitting the realization of low-threshold nanolasers based on TMD monolayers.

Zhang and his colleagues reported a nanolaser by combining a WS\(_2\) monolayer with a WGM cavity. This nanolaser was fabricated by embedding a WS\(_2\) monolayer between dielectric layers of Si\(_3\)N\(_4\) and HSQ to form a WGM cavity (Figure 3a, b).\(^3\) By carefully designing microcavity, a microdisk with a diameter of 3.3 \(\mu\)m was employed, presenting a resonant transverse electric (TE)-polarized WGM at a wavelength of 612 nm (Figure 3c). This resonant mode overlapped with the exciton emission peak and showed a high-quality factor of 2604.
The lasing emissions of WS₂ WGM nanolasers were optically pumped by a 473 nm pulsed laser (190 fs pulse duration, 80 MHz repetition rate) at 10 K. The PL emissions of monolayer WS₂ in cavity shows a clear power dependence: at low pump power intensity below 3.14 MW cm⁻², a broad peak corresponding to spontaneous emission of WS₂ was observed; as the power exceeds 22.4 MW cm⁻², a narrow peak at 612.2 nm appeared, indicating the lasing emission of WS₂ (Figure 3d). The power-dependent emission intensities of a WS₂ nanolaser has been fitted by rate equation, displaying a threshold of ∼5−8 MW cm⁻² and a β factor of 0.5 (Figure 3e). The FWHM as a function of pump intensity also shows a clear narrowing of peak above threshold, demonstrating the transition from spontaneous emission to stimulated lasing emission (Figure 3f). This work represents the first demonstration of a WGM laser based on TMD monolayers. The ultrahigh quality factors of WGM cavities permit the realization of low-threshold lasing emission. Compared to photonic-crystal nanolasers, which are restricted by the self-absorption in III–V or Si semiconductor nanocavities, the introduction of dielectric WGM cavities also circumvent the restriction of material selection.

Besides the microdisks, other categories of WGM cavities can also be employed to construct high-performance nanolasers based on TMDs. Salehzadeh et al. reported a room-temperature laser with multiple lasing modes based on four-layer MoS₂ and a free-standing microdisk and microsphere cavity. The four-layer MoS₂ was employed and treated with O₂ plasma to obtain a direct bandgap. Compared to monolayers, four-layer MoS₂ were selected by considering the suppressed Auger recombination with the increase of thickness. By sandwiching MoS₂ layers between a microdisk and a microsphere, a confined strong optical field can be achieved at the microdisk/microsphere interface. Through 3D finite-difference time-domain (FTDT) simulation, remarkably enhanced electric field at the interface between the SiO₂ microdisk and microsphere were demonstrated, which benefits optical confinement and realization of low-threshold lasing emission. Multi-mode lasing emissions were observed as the pump power exceeds a threshold of 5 μW.

Figure 4. Vertical-cavity surface-emitting lasers based on WS₂ monolayers. (a) Scheme of WS₂ monolayers sandwiched between top and bottom distributed Bragg reflectors (DBRs). (b) Reflection spectra of WS₂ monolayer embedded in DBRs. (c) PL spectrum of WS₂ in a cavity at the excitation power of 100 nW. (d–f) Integrated intensity, width and position of a WS₂ laser as functions of excitation power. (g) Confocal PL scanning at the position of cavity center (black), surface (red), and 5.1 μm (blue), respectively. (h) PL intensities of lasing emission (LE) and leaked spontaneous emission (LSE) at different Z positions. Reproduced from ref 66. Copyright 2017 Springer Nature.
This work demonstrated that lower-threshold and room-
temperature lasing emission can be realized by optimizing the microcavity to create a confined strong optical field.

Passivation of TMD monolayers is another significant approach for lowering the threshold and realization of room-
temperature operation of lasers.96–99 Recently, Liao et al. demonstrated a WGM mode laser with a threshold of 5 W cm$^{-2}$ based on chemical vapor deposition (CVD) grown MoS$_2$.67 Micro/nanofibers were employed as WGM cavity and MoS$_2$ were directly grown onto these cavities by a CVD process. The taper-drawing processing was carried out to fabricate micro/
nanofiber cavities of 1 $\mu$m in diameter from standard fibers of 125 $\mu$m in diameter. In this process, the breaking of siloxane bonds occurs to generate oxygen dangling bonds. The authors demonstrated that these dangling bonds can effectively passivate the defects in MoS$_2$ monolayers under a wide power dynamic range. At low pump power of less than 1 W cm$^{-2}$, the quantum yield of 30% can be achieved. Even under a high pump power of $10^4$ W cm$^{-2}$, a relatively high quantum efficiency exceeding 1% can be reached. In contrast, the MoS$_2$ on planar substrate exhibited quantum yield of less than 0.05%. Well passivated defects in MoS$_2$ benefits the buildup of population inversion at lower power, therefore effectively lowering the lasing threshold of MoS$_2$. By pumping the MoS$_2$ WGM lasers with a 532 nm continuous-wave laser, lasing emission can be observed, which presented a low threshold of 5 W cm$^{-2}$ at room temperature. Above the threshold, this WGM laser exhibited a FWHM of $\sim 1.97$ nm, corresponding to a quality factor of 350. This result indicates that low-threshold lasing emissions are feasible based on well passivated monolayers. For the practical application of TMD-based nanolasers, this work is illuminating because the CVD grown samples is important to the scalable fabrication and on-chip integration of nanolasers.

### VERTICAL-CAVITY SURFACE-EMITTING LASERS

Vertical-cavity surface-emitting lasers (VCSELs) employ distributed Bragg reflectors (DBRs) to achieve a very high reflectivity and strong confinement of photons in a cavity. DBRs are composed of layers with alternating high and low refractive indices and each layer has an optical thickness of $\lambda/4$, where $\lambda$ is optical wavelength. These alternating layers can cause destructive interference at each layer interface, thus giving rise to a stop band for light transmission. With these high-performance reflectors, long cavity photon lifetime of several picoseconds and high quality factor exceeding $10^4$ have been realized in VCSELs.101,102 VCSEL geometry has been employed to realize the lasing emission of III–V semiconductors,103–105 organic materials,106 colloidal quantum dots,107 and biological emitters.108 The optical cavity based on DBRs also provides a platform to study the strong coupling between light and matter.109–111 Exciton polaritons (EPs) and EP Bose–Einstein condensation have been demonstrated in DBR cavities based on III–V materials,103 organic semiconductors,112 and metal-halide perovskites.113

VCSEL geometry is also important for the realization of low-threshold lasing emission of TMD monolayers because of its sub-wavelength cavity length and ultrahigh quality factor. Additionally, embedding TMD monolayers into DBRs also isolate active materials from ambient environment, which benefits the operating stability of lasers. In 2017, Yu and his colleagues demonstrated, for the first time, the VCSELs based on WS$_2$ by continuous-wave excitation at room temperature.66 The lasers were constructed by embedding WS$_2$ monolayers into bottom and top DBRs with 12.5 and 8.5 pairs of SiO$_2$/TiO$_2$ layers, respectively (Figure 4a). These DBRs creates a stop band for light transmission from 590 to 760 nm, which is illustrated in reflection spectrum (Figure 4b). A dip related to a cavity photon mode can be observed at 639.5 nm with a 1.0 ± 0.2 nm, indicating a quality factor of ca. 640. Therefore, these DBRs are capable to confine photons for creating a high-quality optical cavity. Based on this device configuration, a sharp PL peak at 636.3 nm can be observed by pumping with a 532 nm continuous-wave laser, suggesting the stimulated lasing emission of WS$_2$ (Figure 1c). The output intensity as a function of pump power illustrates three obvious regions (Figure 1d). In the first region, PL intensity presents a sublinear relationship with pump power, implying spontaneous exciton emission. The sublinear behavior might be caused by side recombination channels, such as exciton-exciton annihilation under high excitation power. As pump fluence exceeds 4 nW, a superlinear dependence can be observed and a nearly linear dependence can be observed when the pump fluence increases up to 6 nW. This nonlinear response of PL emission strongly evidences the buildup of lasing emission in WS$_2$.

The lasing emission of WS$_2$ was also demonstrated by the power-dependent line width of PL. With the increase of pump fluence, the line width of PL peak decreases from $\sim 1.2$ nm to $\sim 0.6$ nm, while stabilizes at 0.6 nm above the threshold power of 4 nW. The peak position as a function of power illustrates no obvious blueshift with increased power, indicating that this system is a typical photonic laser, instead of exciton–polariton condensation. The lasing behavior of WS$_2$ VCSELs was also demonstrated by confocal PL measurements along Z-direction. With the focal plane at the cavity centre, both the narrow peak related to lasing emission and a board peak corresponding to leaked spontaneous emission can be observed (Figure 1g). The Z-position-dependent PL intensity also indicates that leaked spontaneous emission mainly localized at cavity centre, while the lasing emission is surface emitting. The slower spatial decay of lasing emission indicates its high stability and less diffusion. This work demonstrates low-threshold VCSEL based on TMD monolayers and also creates opportunities to create polariton lasers or electrically pumped lasers based on TMD materials and such a device configuration.

### INTERLAYER-EXCITON LASING BASED ON TMD HETEROSTRUCTURES

Ultrafast charge transfer can boost the formation of spatially indirect interlayer excitons with electrons and holes distributed in two different layers in TMD heterostructures. These interlayer excitons possess intriguing optical properties compared to those of direct excitons in monolayers. Firstly, the interlayer excitons exhibit much longer lifetimes than the intralayer excitons. The longer lifetimes permit the relaxation of excitons into ground states before recombination, thus, hopefully, leading to the realization of exciton–polariton BEC and lasing emission. Secondly, electrons and holes distributed in different layers result in permanent electric dipole moment of interlayer excitons, which benefits the stronger repulsive nonlinear interactions and electric-field-tunable carrier dynamics. The spatially separated electrons and holes also allows for the electric injection from different sides of heterojunctions, which boosts the development of light-emitting diodes and possible electrically pumped lasers.
PHOTONIC LASING BASED ON INTERLAYER EXCITONS

For the lasing emission, type-II TMD heterostructures provide a three-level system, which benefits the buildup of population inversion and low-threshold lasing emission. More importantly, such a device configuration is hopeful to realize lasing emission via electric injection, which is crucial for practical applications. Meanwhile, the relatively lower quantum efficiency stemming from the momentum mismatch and reduced exciton oscillation strength also might be the restriction for the realization of high-performance lasing emissions based on interlayer excitons.

Interlayer excitons possess intriguing optical properties compared to those of direct excitons in monolayers.

Gao and his colleagues firstly demonstrated the interlayer-exciton lasers based on MoS2/WSe2 heterostructures (Figure 5a). The MoS2 and WSe2 can forms type-II band alignment. Ultrafast charge transfer has been demonstrated at the time scale within 50 fs, yielding electrons in MoS2, and holes in WSe2 to form interlayer excitons. Free-standing photonic crystal cavity comprising 220 nm suspended silicon was selected to confine photons with a high-quality factor and MoS2/WSe2 heterostructures were fabricated by dry transfer onto photonic crystals (Figure 5b). The intralayer exciton emissions of MoS2 and WSe2 are centred at 668 and 750 nm, respectively. In contrast, the interlayer excitons exhibit a PL peak at 1128.6 nm, which is out of absorption band of silicon. With the pump power exceeding the threshold, a sharp cavity mode of stimulated emissions of heterostructures can be observed at room temperature (Figure 5c). The FWHM of cavity mode slightly above the lasing threshold is 2.15 nm. The output power as a function of pump power provides a strong evidence of lasing emission (Figure 5d). For cavity mode, an obvious “kink” can be observed, which can be attributed to the nonlinear behavior of lasing emission. In contrast, there is no obvious “kink” in broad spontaneous emissions.

Coherence is another important criterion of lasing emission. The coherent length of MoS2/WSe2 interlayer-exciton lasers were measured by a Michelson interferometer. The visibility is defined as

\[ \nu = \frac{I_{\text{max}}(\Delta \tau) - I_{\text{min}}(\Delta \tau)}{I_{\text{max}}(\Delta \tau) + I_{\text{min}}(\Delta \tau)} \]

where \( I_{\text{max(min)}} \) is the maximum (minimum) intensity of envelop function at delay time of \( \Delta \tau \). The measured visibility as a function of path delay is shown in Figure 5e. The visibility measured in a Michelson interferometer (Figure 5f) indicates that the transition from linear to superlinear increase with the rise of pump power can be observed, indicating the transition from spontaneous to stimulated emissions above the threshold (\( I_\text{p} = 0.18 \mu \text{W} \)). Above the threshold, the line width of lasing emission also experiences a sharp decrease from ~2.4 to ~1.9 meV.

To rigorously identify the lasing behavior, first-order coherence measurements were carried out. The first-order spatial coherence function \( g^{(1)}(r_1, r_2) \) is defined as

\[ g^{(1)}(r_1, r_2) = \frac{G^{(1)}(r_1, r_2)}{\sqrt{G^{(1)}(r_1, r_2)G^{(1)}(r_2, r_2)}} \]

where \( G^{(1)}(r_1, r_2) \) is the first order correlation function, defined as

\[ G^{(1)}(r_1, r_2) = \text{Tr}[\rho E^{-}(r_1)E^{+}(r_2)] \]

BOSE–EINSTEIN CONDENSATION OF INTERLAYER EXCITONS

For dissipative out-of-equilibrium Boson systems, exciton BEC often accompanies with lasing emission, owing to the elementary excitation concentrated into a same ground state. Compared to photonic lasing, which requires population inversion at a relatively high pump density, lasing based on BEC, such as exciton–polariton lasing, often exhibits much lower threshold. Although lasing emission has yet been observed in exciton condensates based on TMD heterostructure system, the realization of exciton BEC suggests the possibility of BEC lasing in the exciton–polariton system after introduction of cavity feedback. Therefore, the development of BEC based on interlayer excitons in TMD heterostructures is feasible to attain electrically pumped lasing based on atomically thin materials with much lower threshold than photonic lasers.
As a typical Boson, excitons are possible to condensate at a ground state. Compared to that of the ultracold dilute atom gas, excitons exhibit a much lower effective mass, which permits the realization of BEC at higher temperature. However, the short lifetime of photoexcited excitons has been a major restriction to realize such macroscopic quantum phase in the exciton system. In the past decades, indirect excitons with spatially separated electrons and holes, such as bilayer quantum well systems and bilayer graphene isolated by hBN, have been demonstrated with BEC. However, exciton condensation was observed under high magnetic field and ultralow temperature in these systems. Recently, a breakthrough of exciton condensation at relatively high temperature of 190 K has been realized in 1T-TiSe$_2$ semimetals. Kogar et al. demonstrated a transition from an electronic, plasmon-like excitation to an exciton condensate by observing falling of the electronic-mode energy to zero at a non-zero momentum using momentum-resolved electron-energy-loss spectroscopy (M-EELS). These results can...
unambiguously demonstrate the BEC phase transition and distinguished the exciton condensate phase from the charge density wave phase originating from Peierls distortion. Although the high-temperature exciton condensation has been realized in this work, the semimetal nature of TiSe₂ restricts its practical implementations toward electroluminescence devices.

The realization of exciton BEC suggests the possibility of BEC lasing in the exciton–polariton system after introduction of cavity feedback.

2D TMD intralayer/interlayer excitons possess exceptionally high binding energy of several hundreds of millielectronvolts, which supports stable exciton resonance under relatively high concentration (>10¹³ cm⁻²) at room temperature. In particular, intralayer excitons with much longer lifetimes than those of interlayer excitons are hopeful to achieve BEC at a ground state. In 2019, Shan, Mak, and their colleagues reported BEC of interlayer excitons in MoSe₂–WSe₂ atomic double layers separated by few-layer hBN at a relatively high temperature of 100 K.¹¹⁹ The device was constructed by inserting two- to three-layer hBN tunneling barrier between MoSe₂ and WSe₂ (Figure 6a). Gate voltages can be applied to tune the electron/hole concentration in MoSe₂/WSe₂ by introducing 20–30 nm hBN as gate dielectrics and few-layer graphene as contact. The reflection spectra of MoSe₂–WSe₂ double layers were shown in Figure 6b. At a bias of 5.5 V, a p–n region with excess electrons in MoSe₂ and excess holes WSe₂ was observed, which reflected by reflection signals at lower energy. This indicates the electroluminescence of interlayer excitons. Based on this device, a high interlayer exciton concentration up to 10¹⁵ cm⁻² can be achieved. The concentration of interlayer excitons is directly related to the tunneling current of the device.

By tuning the gate and bias voltages, the exciton concentration and electroluminescence of MoSe₂–WSe₂ double layers can be controlled. Figure 6c illustrates electroluminescence spectra at different exciton concentrations. These spectra show a peak with a FWHM of 10–20 meV originating from the radiative recombination of interlayer excitons. The integrated intensity of electroluminescence spectra and tunneling current as a function of interlayer exciton concentration were plotted in Figure 6d. The electroluminescence intensity presents a clear threshold at ~0.26 × 10¹² cm⁻². Around the threshold, electroluminescence experiences a rapid increase of two orders of magnitude with the two-fold increase of tunneling current. The second-order correlation function g²(τ) was measured using a Hanbury–Brown–Twiss-type setup to study the coherence of electroluminescence as a function of exciton concentration (Figure 6d). Near the threshold, photon bunching with g²(τ) > 1 has been observed, which is absent (g²(τ) = 1) with the exciton concentration above the threshold. Super-Poissonian photon statistics were observed, indicating the formation of exciton condensation. The threshold behavior together with Poissonian statistics indicates the exciton condensation in MoSe₂–WSe₂ double layers.

In this Review, we have summarized the construction of nanolasers based on TMD monolayers and vdW heterostructures incorporated with various optical cavities. Compared to conventional III–V semiconducting quantum wells and dots, TMDs with tightly bound excitons and atomically thin...
2D TMD intralayer/interlayer excitons possess an exceptionally high binding energy of several hundreds of millielectronvolts, which supports stable exciton resonance under relatively high concentration at room temperature.

structures are potentially good candidates for the ultracompact nanolasers. Narrowed peaks, clear thresholds and first-order coherence have unambiguously distinguished the lasing emissions from the narrowed emissions caused by other mechanisms.\textsuperscript{33,34,63–66} Continuous-wave excitation, room-temperature operation, and relatively low threshold have been realized based on TMD monolayers and vdW heterostructures. Integration of TMD monolayers and heterostructures with silicon photonics has created photonic devices, such as modulators and photodetectors. It is expected that ultracompact integrated photonic circuits can be realized after incorporating nanolasers based on TMD materials. Despite the rapid progress, it still remains challenging for the practical applications of TMD lasers. At the present, almost all of TMD nanolasers discovered are based on samples exfoliated from bulk crystals. Large-area fabrication of high-quality TMD monolayer and heterostructure thin films onto target substrates is a prerequisite for the on-chip integration of TMD nanolasers. Although the CVD-grown samples on silica fibers have presented the lasing emission,\textsuperscript{67} planar integration of coherent light sources requires growth of TMD materials onto planar substrates, such as silicon, Si$_3$N$_4$ and silica plates. For TMD monolayers fabricated by mechanical exfoliation from bulk crystals and CVD method, a large defect density gives rise to a relatively low PL quantum yield below 1%.\textsuperscript{121,122} These defects have caused serious non-radiative recombination, which usually overwhelms the radiative recombination at the room temperature. In particular, TMD monolayers grown by CVD often possess much higher defect density than their mechanically exfoliated counterparts.\textsuperscript{123} Although mechanically exfoliated monolayers often exhibit higher performance, the CVD method plays a pivotal role in the practical device application of TMD monolayers. Therefore, it is significant to develop CVD process to suppress the defect formation and post-treatment techniques for defect passivation. To further decrease the threshold of lasers, rational passivation of traps plays an important role. Some of surface chemical passivation methods have been developed, but high PL quantum yields are only observed under low exciton population and a significant loss of quantum efficiency occurred at high excitation power, which is not suitable for the high-performance lasing applications.

For the practical application of vdW heterostructures, control of crystallographic alignment is an additional requirement. The efficiency of charge transfer and generation of interlayer excitons related to the momentum need to match with each other between the different layers, which has not been extensively investigated in CVD-grown heterostructures. The properties of interlayer excitons in CVD-grown heterostructures have not been well studied and approaches to improve the PL quantum efficiency of interlayer excitons in dash line structures still elusive.

Electrically pumped lasers are another milestone for the development of integrated lasers based on atomically thin TMD heterostructures. At the present stage, continuous-wave lasing emission and electrically injected light-emitting diodes have been realized based on vdW heterostructures. Development of electrically pumped lasing emission requires further optimization of light-emitting layers, charge carrier transport layers and optical cavities. Firstly, improvement of quantum yield by rational passivation is required to realize high quantum efficiency. Secondly, optimization of transport layers and contact between different layers should be carried out to enable the high-intensity charge injection and buildup of enough exciton population to realize lasing emission. Thirdly, conductive optical cavities can be introduced to achieve charge-carrier transport and optical confinement simultaneously. After the realization of electrically pumped lasers, integration of other photonic components, including waveguides, optical modulators and photodetectors, can accelerate the development of ultracompact integrated photonics based on atomically thin TMD materials.

Introduction of spin–valley polarization into lasing emission offers new opportunities to create functional lasing devices. In III–V semiconducting quantum wells, spin polarized lasers have been achieved by employing anisotropic refractive index, magnetic nanoparticles and ferromagnetic Schottky contact.\textsuperscript{101,124,125} Enhanced electron–hole exchange interaction under high population might be the main restriction and the stabilization of spin polarization in TMD materials is still elusive. Fundamental insights into the restriction factors for the valley polarization lifetime are significant for the further development of all valleytronic devices, including the spin-polarized nanolasers.

Development of exciton–polariton lasers based on TMD materials is another important direction to study the low-threshold lasing emission and many-body physics, such as BEC\textsuperscript{100} and superfluidity.\textsuperscript{126–128} In a semiconducting microcavity, strong coupling of excitons and photons creates a kind of new bosonic quasi-particles termed exciton polariton. With efficient energy relaxation, exciton polaritons is capable to concentrate onto one ground state. The exciton polariton condensates are a typical quasi-equilibrium dissipative system and polaritons present a lifetime of 1–10 ps, which can finally emit coherent photons from the same ground state. Because this process does not require population inversion, polariton lasers often exhibit orders-of-magnitude lower thresholds than photonic lasers. Considerable exciton binding energy of several hundreds of millielectronvolt sustain stable exciton polariton at room temperature, whereas exciton polaritons in GaAs semiconducting quantum wells only stabilize at cryogenic temperature owing to their small exciton binding energy less than 10 meV. Strong coupling and formation of exciton polariton have been demonstrated by incorporating TMD monolayers with DBR microcavities. On the basis of this device configuration, spin–valley accessibility of exciton polariton has been demonstrated and electrical injection of exciton polaritons has been realized by loading vdW heterostructures in optical microcavities. Observation of polariton condensation and superfluidity of TMD monolayers and vdW heterostructures will be an exciting direction to be explored in the future. Combination of unique physical properties of TMD materials with the microcavity exciton polaritons is an intriguing direction to realize the manipulation of polaritons and polaritonic condensates by employing helical light, external electric, and magnetic fields.
Complete contact information is available at: https://pubs.acs.org/10.1021/acsmaterialslett.0c00277

Notes
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