

A General Definition of Malware (Talk at Nanyang Technological University)

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Malware example and impact

Conficker worm detected in November 2008—still active—can cause a computer under the Windows operating system to become a component of a remote-controlled **botnet** against the user's will—on an infected computer, it causes a buffer overflow in which harmful excess code is executed by the operating system—the excess code downloads more code that hijacks the server services of the operating system, in order to update and spread the worm via the network—variant code inhibits also the security services of the operating system and connections to anti-malware websites. . . *affected European military systems* . . .

Worldwide malware-induced damage in 2006 $\$13.3 \cdot 10^9$
[Computer Economics Inc., 2007]

Outline

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Malware as harmful software

Harm as incorrectness

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Motivation, Goal, and Methodology

Malware as harmful software
Harm as incorrectness
Prerequisites

Motivation, Goal, and Methodology

Motivation An open problem [FHZ06]: find a general definition of **malware** (= **malicious software**), e.g., botnets, rootkits, Trojan horses, viruses, worms, etc.

Goal Obtain a formal solution to the problem.

Methodology Formulation of the solution as a *single sentence* in a **computational modal fixpoint logic**.

Malware as harmful software

What is malware?

- ▶ Informally,

malware = malicious software

- ▶ Malicious intention is not generally directly observable!
- ▶ How to distinguish *unawareness* (juvenile hacking, accidental anti-hacking) from *malice*?
- ▶ **Users don't care:** all that matters is (harmful) *effect*, not (malicious) intention.
- ▶ **Malice is immaterial!**
- ▶ psychological "definition"

- ▶ Intuitively,

malware = harmful software

- ▶ Harmful effect *is* observable!
- ▶ scientific definition

Harm as incorrectness

- ▶ **doing harm** = causing that

actual behaviour \neq **intended** behaviour

- ▶ **actuality** – **intention** = **incorrectness**

- ▶ **defining principle** for malware:

causation of incorrectness

- ▶ **harmful attack** = falsification of a necessary condition for correctness

- ▶ **formal systems engineering**

- ▶ correctness *intention* must be specified
- ▶ we don't care how:

correct(s)

Example: Sorting

- ▶ **Given:** a program s for sorting an array A of l integers
- ▶ **Sought:** a correctness definition for s
 - ▶ Pre := $A : \text{Array}_{l \in \mathbb{N}}(\mathbb{Z})$
 - ▶ Post := $\forall(1 \leq i \leq l) \forall(1 \leq j \leq l)(i \leq j \rightarrow A[i] \leq A[j])$
 - ▶ correct(s) :iff \vdash_{Hoare} Pre {s} Post
- ▶ **Variations:** add necessary conditions (e.g., exact *algorithmic complexity*), stipulate *proof-carrying code*, etc.

Prerequisites

Theorem (Knaster-Tarski fixpoint theorem)

Let $\langle L, \leq \rangle$ designate a **complete** lattice¹ and $f : L \rightarrow L$ a **monotonic** map² on L . Then,

$$g := \bigvee \{ a \mid a \in L \text{ and } a \leq f(a) \}$$

is the **greatest** fixpoint of f , and, dually,

$$l := \bigwedge \{ a \mid a \in L \text{ and } f(a) \leq a \}$$

is the **least** fixpoint of f .

¹ $\bigvee S$ (lub) and $\bigwedge S$ (glb) exist for **arbitrary** $S \subseteq L$

²for all $a, b \in L$, if $a \leq b$ then $f(a) \leq f(b)$

Preliminaries

Definition (Damaging software)

A software system s **damages** a correct software system s' by definition if and only if s (directly or indirectly) causes incorrectness to s' . Formally,

s damages s'	:iff	$\text{correct}(s')$ and not $\text{correct}(s(s'))$	directly
s damages ⁰ s'	:iff	s damages s'	
s damages ^{$n+1$} s'	:iff	there is s'' s.t. not s'' damages ⁰ s' and $s(s'')$ damages ^{n} s'	indirectly
s damages ^o s'	:iff	$\bigcup_{n \in \mathbb{N}} s$ damages ^{n} s' .	

Malware Logic

Definition (MalLog)

Let \mathcal{M} designate a countable set of propositional variables M , and

$$\Phi \ni \phi ::= M \mid \neg\phi \mid \phi \wedge \phi \mid \forall \mathbf{D}(\phi) \mid \forall \mathbf{R}(\phi) \mid \nu M(\phi)$$

the language Φ of MalLog where all free occurrences of M in ϕ of $\nu M(\phi)$ are assumed to occur within an even number of occurrences of \neg to guarantee the existence of (greatest) fixpoints (expressed by $\nu M(\phi)$) [BS07].

Preliminaries

Definition (Repairing software)

A software system s **repairs** an incorrect software system s' by definition if and only if s (directly or indirectly) causes correctness to s' . Formally,

s repairs s'	:iff	not $\text{correct}(s')$ and $\text{correct}(s(s'))$	directly
s repairs ⁰ s'	:iff	s repairs s'	
s repairs ^{$n+1$} s'	:iff	there is s'' s.t. not s'' repairs ^o s' and $s(s'')$ repairs ^{n} s'	indirectly
s repairs ^o s'	:iff	$\bigcup_{n \in \mathbb{N}} s$ repairs ^{n} s' .	

Malware Logic (continued)

Then, given the (or only some sub-) class \mathcal{S} of software systems (not just pieces of software) s and an interpretation $\llbracket \cdot \rrbracket : \mathcal{M} \rightarrow 2^{\mathcal{S}}$ of propositional variables, the interpretation $\llbracket \cdot \rrbracket : \Phi \rightarrow 2^{\mathcal{S}}$ of MalLog-propositions is:

$$\begin{aligned} \llbracket M \rrbracket &:= \llbracket M \rrbracket \\ \llbracket \neg\phi \rrbracket &:= \mathcal{S} \setminus \llbracket \phi \rrbracket \\ \llbracket \phi \wedge \phi' \rrbracket &:= \llbracket \phi \rrbracket \cap \llbracket \phi' \rrbracket \\ \llbracket \forall \mathbf{D}(\phi) \rrbracket &:= \{ s \mid \text{for all } s', \text{ if } s \text{ damages}^o s' \text{ then } s' \in \llbracket \phi \rrbracket \} \\ \llbracket \forall \mathbf{R}(\phi) \rrbracket &:= \{ s \mid \text{for all } s', \text{ if } s \text{ repairs}^o s' \text{ then } s' \in \llbracket \phi \rrbracket \} \\ \llbracket \nu M(\phi) \rrbracket &:= \bigcup \{ S \mid S \subseteq \llbracket \phi \rrbracket_{[M \mapsto S]} \} \end{aligned}$$

where $\llbracket \cdot \rrbracket_{[M \mapsto S]}$ maps M to S and otherwise agrees with $\llbracket \cdot \rrbracket$.

Malware Logic (continued)

Further, $\phi \vee \phi' := \neg(\neg\phi \wedge \neg\phi')$, $\top := \phi \vee \neg\phi$, $\perp := \neg\top$,
 $\phi \rightarrow \phi' := \neg\phi \vee \phi'$, $\phi \leftrightarrow \phi' := (\phi \rightarrow \phi') \wedge (\phi' \rightarrow \phi)$, and

$$\begin{aligned}\exists\mathbf{D}(\phi) &:= \neg\forall\mathbf{D}(\neg\phi) \\ \exists\mathbf{R}(\phi) &:= \neg\forall\mathbf{R}(\neg\phi) \\ \mu M(\phi(M)) &:= \neg\nu M(\neg\phi(\neg M)).\end{aligned}$$

Finally,

- ▶ for all $\phi \in \Phi$ and $s \in \mathcal{S}$, $s \models \phi$:iff $s \in \|\phi\|_{[\cdot]}$
- ▶ $\models \phi$:iff for all $s \in \mathcal{S}$, $s \models \phi$
- ▶ for all $\phi, \phi' \in \Phi$,
 - ▶ $\phi \Rightarrow \phi'$:iff for all $s \in \mathcal{S}$, if $s \models \phi$ then $s \models \phi'$
 - ▶ $\phi \Leftrightarrow \phi'$:iff $\phi \Rightarrow \phi'$ and $\phi' \Rightarrow \phi$.

Basic properties of MalLog (continued)

Corollary

1. If damages^o and repairs^o are **decidable** on a given software systems domain then the satisfiability problem for MalLog, i.e., “Given $\phi \in \Phi$, is there $s \in \mathcal{S}$ s.t. $s \models \phi$?”, (and thus also the model-checking problem, i.e., “Given $\phi \in \Phi$ and $s \in \mathcal{S}$, is it the case that $s \models \phi$?”) is decidable.
2. MalLog is **axiomatisable** by the following Hilbert-style proof-system:
 - 2.1 the axioms/rules of the modal system **K** for each $\forall\mathbf{D}$ and $\forall\mathbf{R}$
 - 2.2 the axiom $\frac{\phi(\mu M(\phi(M)))}{\phi(\mu M(\phi(M)))} \rightarrow \mu M(\phi(M))$
 - 2.3 the rule $\frac{\phi(\phi') \rightarrow \phi'}{\mu M(\phi(M)) \rightarrow \phi'}$.

Basic properties of MalLog

Fact

1. $\models \phi \rightarrow \phi'$ iff $\phi \Rightarrow \phi'$
(By expansion of the definitions.)
2. $\models \phi \leftrightarrow \phi'$ iff $\phi \Leftrightarrow \phi'$
3. MalLog is a member of the family of μ -calculi over the modal system **K**₂, which is characterised by the validities of propositional logic and the modal laws
 $\models \Box(\phi \rightarrow \phi') \rightarrow (\Box\phi \rightarrow \Box\phi')$ and “if $\models \phi$ then $\models \Box\phi$ ”, where $\Box \in \{\forall\mathbf{D}, \forall\mathbf{R}\}$.

Defining malware

Definition (Malware)

A software system s is **malware** by definition if and only if s damages non-damaging software systems (the *civil population* so to say) or software systems that damage malware (the *anti-terror force* so to say). Formally,

$$\text{mal}(s) \quad \text{:iff} \quad s \models \nu M(\exists\mathbf{D}(\forall\mathbf{D}(M)))$$

An iterative paraphrase

- ▶ Everything is malware (better be safe than sorry)
- ▶ except for (throw **out** what is clearly safe) the following systems:

0. non-damaging systems (CP)
1. systems that damage only systems that damage CP (ATF1)
2. systems that damage only systems that damage ATF1 (ATF2)
3. systems that damage only systems that damage ATF2 (ATF3)
4. etc.

An iterative paraphrase

- ▶ Nothing is benware (again, better be safe than sorry)
- ▶ except for (throw **in** what is clearly safe) the following systems:

0. non-damaging systems (CP)
1. systems that damage only systems that damage CP (ATF1)
2. systems that damage only systems that damage ATF1 (ATF2)
3. systems that damage only systems that damage ATF2 (ATF3)
4. etc.

Deriving benware

Definition (Benware)

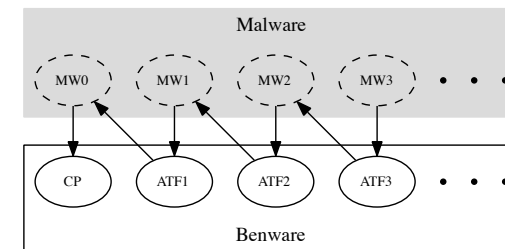
A software system s is **benware** by definition if and only if s is non-damaging or damages only software systems that damage benware. Formally,

$$\text{ben}(s) \text{ :iff } s \models \mu M(\lambda D(\exists D(M)))$$

The Malware-versus-Benware **arms race**

Fact

$\text{ben}(s)$ if and only if not $\text{mal}(s)$



Good&Bad distinction induced by the existence of a population that is (perceived as) non-damaging

Anti-malware

Definition (Anti-malware)

A software system s is **anti-malware** by definition if and only if s damages no benware (safety)³ and s neutralises⁴ malware (effectiveness). Formally,

$$\text{antimal}(s) \text{ :iff } s \models \neg \exists \mathbf{D}(\text{BEN}) \text{ and} \\ \text{there is } s' \text{ s.t. } \text{mal}(s') \text{ and not } \text{mal}(s(s'))$$

where $\text{BEN} := \mu M(\forall \mathbf{D}(\exists \mathbf{D}(M)))$.

³no friendly fire

⁴Damage is insufficient!

Medware

Definition (Medware)

A software system s is **medware** by definition if and only if s damages no benware (safety) and s repairs benware (effectiveness). Formally,

$$\text{med}(s) \text{ :iff } s \models \neg \exists \mathbf{D}(\text{BEN}) \wedge \exists \mathbf{R}(\text{BEN}).$$

Tasks, Tools, and Techniques for fighting Malware

Task	Tool	Technique
detection	satisfaction relation \models	Model Checking
comparison	language & bisimulation equivalence	Equivalence Checking
classification	characteristic formulas	MC, EC

Malware Comparison (declarative)

Definition (Language equivalence)

For all $s_1, s_2 \in \mathcal{S}$,

- ▶ $s_1 \sqsubseteq_{\Phi} s_2$:iff for all $\phi \in \Phi$, if $s_1 \models \phi$ then $s_2 \models \phi$
- ▶ $s_1 \equiv_{\Phi} s_2$:iff $s_1 \sqsubseteq_{\Phi} s_2$ and $s_2 \sqsubseteq_{\Phi} s_1$.

Malware Comparison (operational)

Definition (Bisimulation equivalence)

- ▶ For all $s_1, s_2 \in \mathcal{S}$,
 - ▶ $s_1 \sqsubseteq s_2$ iff for all $s'_1 \in \mathcal{S}$,
 1. if $s_1 \text{ damages}^\circ s'_1$ then there is $s'_2 \in \mathcal{S}$ s.t. $s_2 \text{ damages}^\circ s'_2$
 2. if $s_1 \text{ repairs}^\circ s'_1$ then there is $s'_2 \in \mathcal{S}$ s.t. $s_2 \text{ repairs}^\circ s'_2$.
- ▶ For all $S \subseteq \mathcal{S} \times \mathcal{S}$,

$$\mathcal{O}_{\sqsubseteq}(S) := \{ (s_1, s_2) \mid (s_1, s_2) \in S \text{ and } s_1 \sqsubseteq s_2 \text{ and } s_2 \sqsubseteq s_1 \}.$$
- ▶ $\approx :=$ the greatest fixpoint of (monotonic) $\mathcal{O}_{\sqsubseteq}$
 $= \bigcup \{ S \mid S \subseteq \mathcal{O}_{\sqsubseteq}(S) \}$, by Knaster-Tarski

Characterisation result

Theorem

For all $s, s' \in \mathcal{S}$,

$$s \equiv_{\Phi} s' \text{ iff } s \approx s' \text{ iff } s \models \chi(s', \mathcal{S}).$$

Malware Classification

Definition (Characteristic formula)

Let $S \subseteq \mathcal{S}$, $s \in \mathcal{S}$, $D(S, s) := \{ s' \mid s' \in S \text{ and } s \text{ damages}^\circ s' \}$,
 $R(S, s) := \{ s' \mid s' \in S \text{ and } s \text{ repairs}^\circ s' \}$, and $M_s \in \mathcal{M}$. Then,
 the **characteristic formula** $\chi(s, S)$ of the software system s w.r.t.
 S is the solution of the equation system

$$M_s \stackrel{\nu}{=} \forall \mathbf{D}(\bigvee_{s' \in D(S, s)} M_{s'}) \wedge \forall \mathbf{R}(\bigvee_{s' \in R(S, s)} M_{s'}) \wedge \\ [\bigwedge_{s' \in D(S, s)} \exists \mathbf{D}(M_{s'})] \wedge [\bigwedge_{s' \in R(S, s)} \exists \mathbf{R}(M_{s'})],$$

(where $\bigvee \emptyset := \perp$ and $\bigwedge \emptyset := \top$) obtained [BS07] by translating
 each equation $M^i \stackrel{\nu}{=} \psi^i(S)$ into a formula $\nu M^i(\psi^i(S))$ and
 recursively substituting these formulae for the corresponding free
 variables in the first formula $\nu M_s(\psi_s(S))$.

Assessment

Our approach:

1. malware-versus-benware arms race confined to formal systems engineering
2. malware detection \rightsquigarrow automated systems verification
3. system security \rightsquigarrow system correctness
4. generic (predicate correct is a *plug-in*)
5. **hacker-safe:**




no recipe for malware construction derivable

Related work

About viruses only, not hacker-safe (constructive):

1. Adleman: Gödel-numberings [Adl88]
2. Cohen: Turing-machines [Coh87]
3. Bonfante et al.: Kleene Recursion Theorem [BKM06]

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Future work

Refinements:

- ▶ add **time** (temporal modalities): malware *evolution*
- ▶ add **measure**: *degrees of damage*, malware *cost*

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質問

質問がありますか。

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